

The Applicability of Field Theories in The Population Sciences

MPDE 2017

Based on work by James Wilsenach, Pietro Landi & Cang Hui

7 September



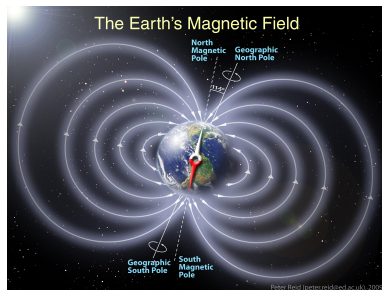
Wilsenach, J., Landi, P., & Hui, C. (2017). Evolutionary fields can explain patterns of high-dimensional complexity in ecology. *Physical Review E*, 95(4), 042401.

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The Field Concept in Physics

- Creates action at a distance
- Is pervasive
- Events are co-dependent and multi-directional
- Particles as persistent events

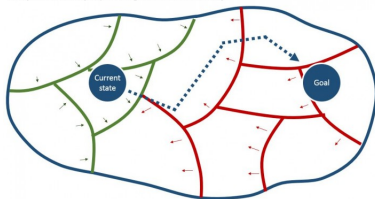


[NASA, 2017]

The Field Interpretation of Sociological Change

- Dynamic
- Driven by motivation
- Consistent Universal Framework
- Qualitative
- Networks similar to Ecology

A depiction of a life space, reflecting Kurt Lewin's field theory



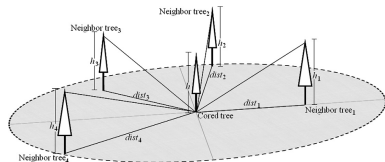
Adapted from Barnes & Cook (2013), Kurt Lewin's Field Theory: A Review and Re-evaluation,
International Journal of Management Reviews, Vol. 15, 408-425
www.interscience.wiley.com

Relationships Between Tree Growth & Spacing

- Familiar inverse square law

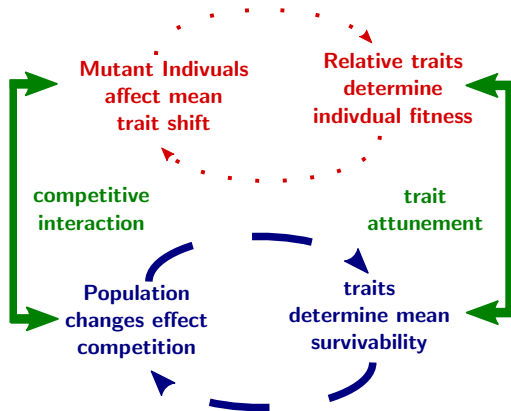
Relationships Between Tree Growth & Spacing

- Familiar inverse square law
- static predictors
- widely used



[Contreras et al., 2011]

What We Mean by Evolutionary Dynamics



What is a Field?

Field Theories in The Population Sciences

Evolutionary Dynamics as a Field Phenomenon

Exploring Predator-Prey Systems

Complexity & Dimensionality

Evolution as a Dynamic Field

Evolution as a Dynamic Field

- 1 An Evolutionary Field Φ depends locally on:
 - Interaction frequency
 $m_i m_j$
 - ecological relationships
 k_{ij}
 - trait attunement $\frac{k_{ij}}{d_{ij}^2}$

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- 2 Φ Influences
 - 1 Trait space topology
 - 2 trait attunement
 - 3 community composition

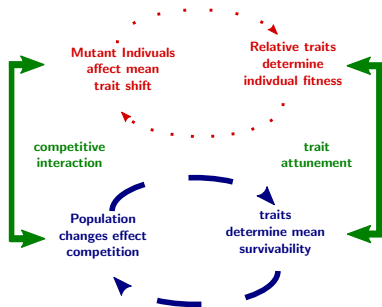
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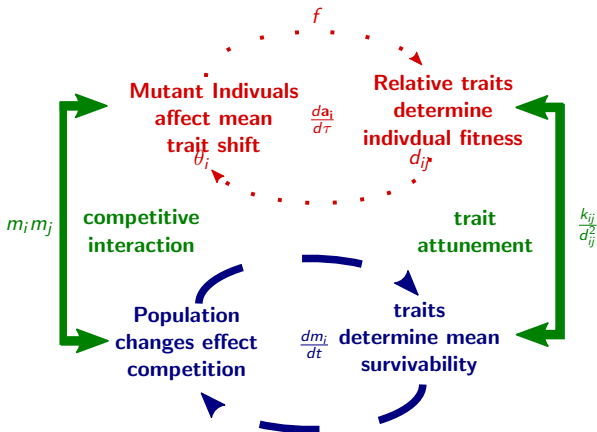
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Evolution as a Dynamic Field



What is a Field?

Field Theories in The Population Sciences
Evolutionary Dynamics as a Field Phenomenon
Exploring Predator-Prey Systems
Complexity & Dimensionality

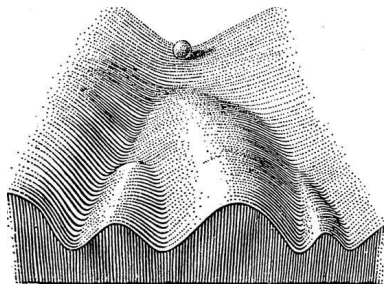
Trait Space Topology

Trait Space Topology

- many possibilities
- assortative selection:

$$d_{ij}^2 = e^{-\|\mathbf{a}_i - \mathbf{a}_j\|^2}$$

- not explosive
- versatile



[Goldberg et al., 2007]

What is a Field?

Field Theories in The Population Sciences

Evolutionary Dynamics as a Field Phenomenon

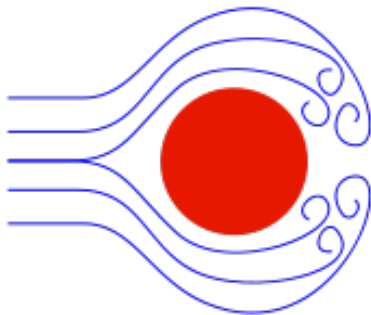
Exploring Predator-Prey Systems

Complexity & Dimensionality

Constraints on Evolutionary Acceleration

Constraints on Evolutionary Acceleration

- mutation pool limits rapid adaptation
 - $\theta_i = \mu_i m_i$
 - versatile
- drags on evolution
 - $f \propto v_i^2$
 - generational/spatial
 - terminal velocity



Field & Motion Equations

$$\Phi_i = \sum_{j=1}^N \frac{k_{ij} m_i m_j}{d_{ij}^2} \mathbf{u}(\mathbf{a}_j, \mathbf{a}_i) \quad (1)$$

$$\frac{d^2 \mathbf{a}_i}{d\tau^2} = \theta_i \left[\sum_{j=1}^N \frac{k_{ij} m_i m_j}{d_{ij}^2} \mathbf{u}(\mathbf{a}_j, \mathbf{a}_i) - \mathbf{f}_i \right] \quad (2)$$

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Fox and Rabbit Case Study

 k_{ij} 

$$k_{11} < 0$$

←→

$$k_{21} < 0$$

→→



$$k_{12} < 0$$

←←

$$k_{22} < 0$$

←→



$$k_{1s} > 0$$

→●

$$k_{1s} = 0$$

Population Dynamics

$$\frac{dm_1}{dt} = \left[r_1 + k_{11}m_1 + \frac{k_{12}}{d_{12}^2}m_2 + \frac{k_{1s}}{d_{1s}^2}m_s \right] m_1 \quad (3)$$

$$\frac{dm_2}{dt} = \left[r_2 + k_{22}m_2 + \frac{k_{21}}{d_{21}^2}m_1 \right] m_2 \quad (4)$$

Population Dynamics

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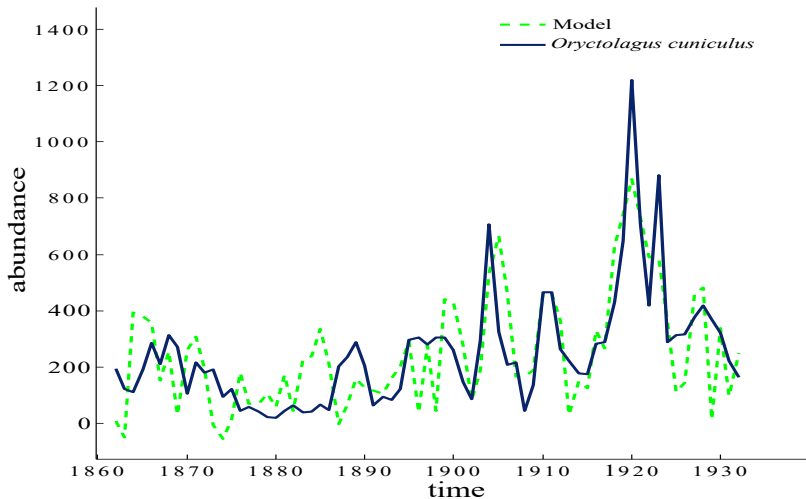
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Population Dynamics

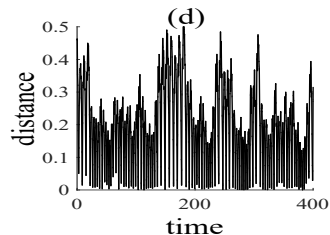
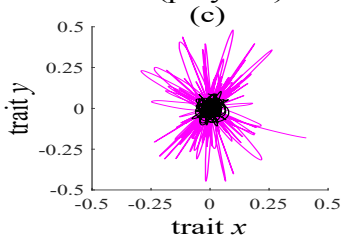
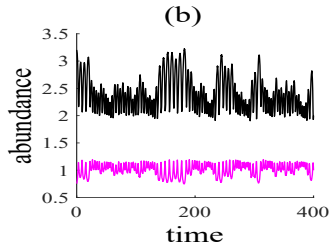
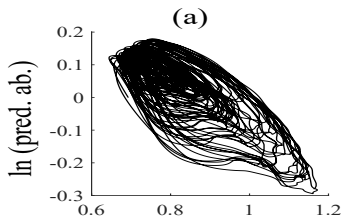
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Model Fit to Rabbit Data

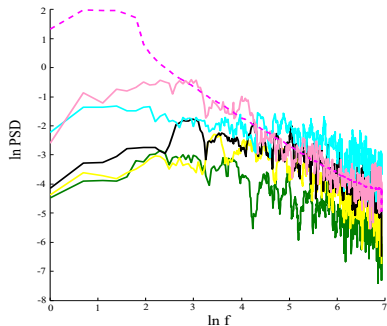





General System Behaviour



Properties of Pink Noise

- everywhere in ecology
- long memory
- fractal dimension $\frac{2}{\alpha-1}$



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